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# Structure of (2R,5R,8S,11S)-1,4,7,10-Tetrabenzyl-2,5,8,11-tetraethyl-1,4,7,10tetraazacyclododecane 

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Abstract. $\mathrm{C}_{44} \mathrm{H}_{60} \mathrm{~N}_{4}$, monoclinic, $P 2_{1} / c, a=9.345$ (4), $b=9.327$ (4), $c=22.358$ (11) $\AA, \beta=94.14$ (8) ${ }^{\circ}, U=$ 1944 (2) $\AA^{3}, D_{m}=1 \cdot 11, D_{c}=1 \cdot 10 \mathrm{Mg} \mathrm{m}^{-3}, Z=2$. The 12 -membered ring forms an armchair conformation with the methylene groups at the top and the toe.

Introduction. This paper forms part of a series of investigations on the cyclic tetramers of chiral aziridines. These tetramers can be divided into four geometrical isomers as shown below (Tsuboyama, Tsuboyama, Uzawa \& Higashi, 1974).





Recently, the two crystal structures with $C_{4}$ symmetry, i.e. $(2 R, 5 R, 8 R, 11 R)-2,5,8,11$-tetraethyl-1,4,7,10-tetraazacyclododecane (TETA) (Sakurai, Kobayashi, Tsuboyama \& Tsuboyama, 1978a), and ( $2 R S, 5 R S, 8 R S, 11 R S$ )-1,4,7,10-tetrabenzyl-2,5,8,11-tetraethyl-1,4,7,10-tetraazacyclododecane ( $R R R R$ type) (Sakurai, Kobayashi, Tsuboyama \& Tsuboyama, $1978 b$ ) were reported. In this paper the structure of the title compound with $C_{i}$ symmetry ( $R R S S$-type) is described.

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Triclinic single crystals were obtained from benzene solution (Tsuboyama et al., 1974). However, many of these crystals were twinned or disordered and were not suitable for the structural work. Therefore they were recrystallized from dioxane solution, and a different crystal form was obtained. The new crystals belong to the monoclinic system $P 2_{1} / c$ with $Z=2$, and possess intramolecular centrosymmetry. The size of the crystal used was $0.4 \times 0.4 \times 0.45 \mathrm{~mm}$. X-ray diffraction data were measured on a Rigaku automated AFC fourcircle diffractometer with graphite-monochromatized Mo $K a$ radiation. Within the range $2 \theta \leq 50^{\circ}, 2132$ independent reflections were observed. The intensities were corrected for Lorentz and polarization factors, but no absorption correction was applied.

The structure was solved by the direct phasing method, and all H atoms were deduced from successive difference Fourier syntheses. The structure was refined by the block-diagonal least-squares method. Unit weight was given to all reflections, and anisotropic temperature factors were used for all non-hydrogen atoms. The final $R$ index was $4 \cdot 8 \%$. Atomic parameters are given in Table $1 . \dagger$

Discussion. A stereoscopic drawing of the molecule is shown in Fig. 1. When projected on the mean plane of

[^0]Table 1. Atomic parameters
Positional parameters are multiplied by $10^{4}$ for $\mathrm{C}, \mathrm{N}, \mathrm{O}$ atoms, and by $10^{3}$ for H atoms. The equivalent temperature factors $\left(\AA^{2}\right)$ are given in the last column. The numbering scheme of the atoms is shown in Fig. 2, and the H atoms are represented by the numbering of the attached C atoms.

|  | $x$ | $y$ | $z$ | $B_{\text {eq }}$ |
| :---: | :---: | :---: | :---: | :---: |
| N(1) | 2124 (2) | -920 (2) | -478 (1) | $3 \cdot 1$ |
| N(4) | 1266 (2) | 1721 (2) | 380 (1) | $3 \cdot 1$ |
| C (2) | 2053 (3) | -792 (3) | 177 (1) | $3 \cdot 1$ |
| C(3) | 2485 (3) | 734 (3) | 374 (1) | $3 \cdot 3$ |
| C(5) | 377 (3) | 1459 (3) | 892 (1) | $3 \cdot 3$ |
| C(6) | -1152 (3) | 2006 (3) | 754 (1) | 3.4 |
| C(2)1 | 2940 (3) | -1921 (3) | 539 (1) | 4.6 |
| C(2)2 | 2634 (4) | -1989 (4) | 1196 (1) | $6 \cdot 3$ |
| $\mathrm{C}(5) 1$ | 1018 (3) | 2042 (4) | 1498 (1) | $5 \cdot 0$ |
| $\mathrm{C}(5) 2$ | 345 (4) | 1332 (5) | 2026 (1) | $8 \cdot 0$ |
| $\mathrm{C}(1) 1$ | 3576 (3) | -1095 (3) | -669 (1) | 3.6 |
| $\mathrm{C}(1) 2$ | 3658 (3) | -681 (3) | -1316 (1) | $3 \cdot 6$ |
| C(1)3 | 4277 (3) | -1571 (3) | -1717(1) | 4.9 |
| $\mathrm{C}(1) 4$ | 4328 (4) | -1188(4) | -2316 (2) | $6 \cdot 3$ |
| C(1)5 | 3782 (4) | 94 (4) | -2513 (1) | $6 \cdot 1$ |
| C(1)6 | 3176 (4) | 1002 (4) | -2118 (1) | $5 \cdot 6$ |
| $\mathrm{C}(1) 7$ | 3122 (3) | 617 (3) | -1528 (1) | 4.6 |
| $\mathrm{C}(4) 1$ | 1774 (3) | 3208 (3) | 359 (1) | 3.7 |
| $\mathrm{C}(4) 2$ | 2100 (3) | 3648 (3) | -266 (1) | 3.7 |
| C(4)3 | 3475 (3) | 4009 (3) | -399 (1) | 4.6 |
| C(4)4 | 3751 (4) | 4462 (3) | -971 (2) | 5.7 |
| C(4)5 | 2658 (4) | 4555 (3) | -1410 (1) | $5 \cdot 7$ |
| $\mathrm{C}(4) 6$ | 1284 (4) | 4186 (4) | -1284 (1) | 5.5 |
| $\mathrm{C}(4) 7$ | 1009 (3) | 3738 (3) | -715 (1) | 4.5 |
| $\mathrm{H}(1) 1$ | 425 (2) | -41 (2) | -40 (1) | $3 \cdot 1$ (0.5) |
| H(1)2 | 400 (2) | -210 (2) | -60 (1) | 3.5 (0.5) |
| H(1)3 | 470 (3) | -249 (3) | -157(1) | $6 \cdot 1$ (0.7) |
| H(1)4 | 482 (4) | -183 (4) | -257(2) | 8.7 (1.0) |
| H(1)5 | 378 (3) | 35 (4) | -295 (1) | 7.8 (0.9) |
| $\mathrm{H}(1) 6$ | 274 (3) | 192 (4) | -227 (1) | 8.3 (0.9) |
| $\mathrm{H}(1) 7$ | 264 (3) | 119 (3) | -126(1) | 5.2 (0.7) |
| H(2) 1 | 97 (2) | -92 (2) | 26 (1) | 3.2 (0.5) |
| H(2)2 | 273 (3) | -285 (3) | 36 (1) | $4 \cdot 2$ (0.6) |
| H(2)3 | 404 (3) | -174 (3) | 51 (1) | $6 \cdot 6$ (0.8) |
| H(2) 4 | 164 (3) | -212 (3) | 129 (1) | 7.4 (0.8) |
| H(2) 5 | 293 (4) | -111(4) | 143 (2) | 9.7 (1.0) |
| H(2)6 | 312 (4) | -283 (4) | 139 (2) | 9.5 (1.0) |
| H(3) 1 | 308 (3) | 71 (3) | 78 (1) | 4.5 (0.6) |
| H(3)2 | 316 (2) | 116 (2) | 8 (1) | 3.1 (0.5) |
| H(4) 1 | 98 (2) | 389 (3) | 49 (1) | 3.9 (0.6) |
| H(4)2 | 269 (2) | 337 (3) | 66 (1) | $4 \cdot 2$ (0.6) |
| H(4)3 | 427 (2) | 393 (3) | -8(1) | 4.7 (0.6) |
| H(4)4 | 478 (3) | 472 (3) | -105 (1) | 6.9 (0.8) |
| H(4)5 | 284 (3) | 489 (3) | -180 (1) | $7 \cdot 2$ (0.8) |
| H(4)6 | 48 (3) | 426 (3) | -160 (1) | $5 \cdot 6$ (0.7) |
| H(4) 7 | 4 (3) | 348 (3) | -63 (1) | 4.9 (0.6) |
| H(5)1 | 29 (2) | 37 (2) | 94 (1) | 2.3 (0.4) |
| H(5)2 | 205 (3) | 183 (3) | 154 (1) | 5.0 (0.6) |
| H(5)3 | 91 (3) | 312 (3) | 149 (1) | 5.5 (0.7) |
| H(5)4 | -72 (4) | 167 (4) | 204 (2) | 12.1(1.2) |
| H(5)5 | 73 (4) | 181 (5) | 241 (2) | 12.0 (1.3) |
| H(5)6 | 60 (3) | 36 (3) | 203 (1) | 6.9 (0.8) |
| H(6) 1 | -152(2) | 231 (2) | 114 (1) | 3.3 (0.5) |
| H(6)2 | -114(2) | 295 (3) | 51 (1) | 3.7 (0.5) |

the 12 -membered ring, the skeleton of the molecule appeared to be a distorted square ring with the methylene groups at the corners (Fig. 2a). However,
the two torsion angles at the $\mathrm{C}(6)$ corner are gauche and -gauche. The ring conformation then is quite different from the $R R R R$-type, and takes an armchair form with $C\left(6^{\prime}\right)$ and $C(6)$ at the top and the toe respectively (Fig. $2 b$ ). The torsion angles and the bond lengths and angles are shown in Fig. 3. The important torsion angles in the ring, together with those in the $R R R R$ type and TETA molecules, are compared in Table 2. The deviations of these torsion angles for the $R R S S$ type from the expected values of the trans and gauche conformations are larger than those of the others. The bond angles $\mathrm{C}(n+1)-\mathrm{C}(n+1) 1-\mathrm{C}(n+1) 2(n=1$ or $4)$, of the ethyl groups, and $\mathrm{N}(n)-\mathrm{C}(n) 1-\mathrm{C}(n) 2(n=1)$ or 4), of the benzyl groups, are several degrees larger than the standard tetrahedral angle of $109.4^{\circ}$. Therefore, it is supposed that the strain energy of the present molecule is higher than that of the $R R R R$-type.


Fig. 1. A stereoscopic drawing of the molecule.

(a)


Fig. 2. The skeleton of the molecule. (a) The projection on the mean plane of the 12 -membered ring. (b) The armchair view.



Fig. 3. (a) Torsion angles $\left({ }^{\circ}\right)$. $(b)$ Bond lengths $(\AA)$ and angles $\left({ }^{\circ}\right)$. $(c)$ Bond lengths $(\mathrm{A})$ and angles $\left({ }^{\circ}\right)$ in the benzyl group. These are the mean values for the two independent groups.

Table 2. The significant torsion angles $\left(^{\circ}\right.$ ) within the 12 -membered ring

|  |  |  |  |  |
| :--- | ---: | ---: | ---: | :---: |
|  | Tetrabenzyltetraethyl- |  |  |  |
| tetraazacyclododecane | TETA |  |  |  |
|  | $n=1$ | $n R S S$-type | $R R R R$-type | molecule |
|  | $n=4$ |  |  |  |
| $\mathrm{C}(n-1)-\mathrm{N}(n)-\mathrm{C}(n+1)-\mathrm{C}(n+2)$ | $-153 \cdot 0$ | $-155 \cdot 9$ | 66. | 166. |
| $\mathrm{~N}(n)-\mathrm{C}(n+1)-\mathrm{C}(n+2)-\mathrm{C}(n+3)$ | $91 \cdot 4$ | $90 \cdot 7$ | -161. | -63. |
| $\mathrm{C}(n+1)-\mathrm{C}(n+2)-\mathrm{N}(n+3)-\mathrm{C}(n+4)$ | $74 \cdot 1$ | $-83 \cdot 4$ | 70. | -75. |

The ${ }^{13} \mathrm{C}$ NMR spectra indicated that the ring skeleton probably retains a single kind of conformation based on the symmetry of the molecule (Tsuboyama, Tsuboyama, Uzawa, Kobayashi \& Sakurai, 1977). In order to see the flexibility of the benzyl group, the conformational energy was calculated with respect to the rotation about the two single bonds in the benzyl group. The Lennard-Jones-type nonbonded interaction was used for the calculation (Sakurai, 1978). Throughout this calculation, the torsion angles about the four groups were changed simultaneously, so that the molecular shape always kept $C_{i}$ symmetry. The resultant energy map has two minima, $A$ and $B$, and the observed structure is within the lowest energy region $A$ (Fig. 4). In this structure, the $\mathrm{C}(n+1)-\mathrm{N}(n)-\mathrm{C}(n) 1-$ $\mathrm{C}(n) 2$ bond is trans and the phenyl plane extends out from the skeleton, while for the second minimum $B$, the corresponding torsion angle is gauche, and the phenyl plane comes closer to the skeleton, as shown in the stereoscopic drawing (Fig. 5). However, the energy barrier between these two minima is larger than that in the $R R R R$-type, and the temperature dependency of the


Fig. 4. The conformational-energy map. The molecule was assumed to keep $C_{i}$ symmetry. The contour lines are drawn at intervals of $5 \mathrm{kcal} \mathrm{mol}^{-1}\left(1 \mathrm{kcal} \mathrm{mol}^{-1} \equiv 4.2 \mathrm{~kJ} \mathrm{~mol}^{-1}\right)$. The observed value is marked by a full circle.

NMR spectra also shows that the $R R S S$-type skeleton is more rigid than the $R R R R$-type. Therefore, the conformation near the minimum $A$ will be maintained in solution.


Fig. 5. A stereoscopic drawing of the molecular model at the subsidiary minimum $B$.


Fig. 6. Packing view of the crystal structure ( $a$-axis projection).

The packing of the molecules in the crystal is shown in Fig. 6. None of the intermolecular $\mathrm{C}-\mathrm{C}$ distances is shorter than $3.7 \AA$, and the main interactions are
between the phenyl groups, as shown by the broken lines in Fig. 6.

Calculations were performed on a FACOM 230-75 computer of this Institute using the UNICS II program system (Sakurai, Iwasaki, Watanabe, Kobayashi, Bando \& Nakamichi, 1974) for crystallography, $L S A M$ (Main, Woolfson \& Germain, 1972) for the direct phasing, and $M M B$ (Sakurai \& Kobayashi, 1972; Sakurai, 1978) for the conformational-energy calculation.

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# 17 $\beta$-Hydroxy- $5 \alpha$-androst-1-en-3-one Hydrate* 

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#### Abstract

C}_{19} \mathrm{H}_{28} \mathrm{O}_{2} . \mathrm{H}_{2} \mathrm{O}, M_{r}=306 \cdot 4, \rho_{x}=1 \cdot 194 \mathrm{Mg}\) $\mathrm{m}^{-3}$, monoclinic, $P 2_{1}, Z=2, a=10.5592$ (6), $b=$ 7.8881 (4), $c=10.2462$ (6) $\AA, \beta=92.345(5)^{\circ}, V=$ $852.71 \AA^{3}$. Final $R=0.058$ for 1727 independent reflections. The $5 a$ sofa conformation of the $\Delta^{1}$-3-one $A$ ring does not produce the type of convexity needed to explain the $1 a$ stereoselectivity of methyl Grignard


[^1]addition. The $C$ (19) angular methyl hydrogens provide a steric cover for the $\beta$ face of $\mathrm{C}(1)$, blocking approach from this direction by the reagent, while the $C(1)$ a face is relatively open to attack.

Introduction. Attempts to explain the stereospecificity of conjugate addition reactions to $\Delta^{1}$ - 3 -one steroids have produced much speculation about the $A$-ring conformations of the precursor molecules and the resulting $\mathrm{C}(1)$ alkylated steroids. For example, Kirk \& © 1979 International Union of Crystallography


[^0]:    $\dagger$ Lists of structure factors and anisotropic temperature factors have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 34202 (14 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.
    (C) 1979 International Union of Crystallography

[^1]:    * Conformational Analysis of Synthetic Androgens. III.
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